

Sixth Semester B.E. Degree Examination, December 2010
Digital Signal Processing

Time: 3 hrs.

Max. Marks:100

- Note: 1. Answer any FIVE full questions,
 selecting at least TWO questions from each part.
 2. Normalized Butterworth letter table may be provided.**

PART – A

- 1 a. State and prove the following properties of DFT.
 - i) Linearity
 - ii) Frequency shifting. (06 Marks)
- b. Compute the circular convolution between the following sequences using DFT and IDFT methods
 $x[n] = (1, 2, 3, 4)$ and $y[n] = (-1, -2, -3, -4)$. $x[n]$ and $y[n]$ are periodic sequences with period $N = 4$. (14 Marks)
- 2 a. Explain the concept of Overlap – Add method, with the necessary diagram. (08 Marks)
- b. Compute the N pt DFT of a^n and $a. n$. (12 Marks)
- 3 a. Find the DFT of $x[n] = [1, 2, 3, 4, 4, 3, 2, 1]$ using the DIT– FFT algorithm. (10 Marks)
- b. Develop an 8 point DIF–FFT algorithm, starting from DFT. State clearly all the steps. Explain how it reduces the number of computations. (10 Marks)
- 4 a. Obtain the direct form–I, direct form–II, cascade and parallel form realizations for the following system :
 $y[n] = 0.75 y[n - 1] - 0.125 y[n - 2] + 6x[n] + 7x[n - 1] + x[n - 2]$. (14 Marks)
- b. Describe with necessary diagram and equations, the linear phase structure of FIR filter for even order. (06 Marks)

PART – B

- 5 a. Let $H_a(s) = \frac{b}{(s+a)^2 + b^2}$ be a causal second order analog transfer function. Show that the causal second order digital filter transfer function $H(t)$, obtained from $H_a(s)$, through impulse invariance method is given by

$$H(t) = \frac{e^{-aT} \sin bT t^{-1}}{1 - 2e^{-aT} \cos bT t^{-1} + e^{-2aT} t^{-2}}$$
 Also find $H(z)$ when $H_a(s) = \frac{1}{s^2 + 2s + 2}$. (12 Marks)
- b. The system function of the analog filter is given as

$$H_a(s) = \frac{s + 0.1}{(s + 0.1)^2 + 16}$$
 Obtain the system function of the digital filter, using bilinear transformation, which is resonant at $\omega_r = \pi/2$. (08 Marks)

- 6 a. Design a Butterworth analog high pass filter, that will meet the following specifications :
- i) Maximum passband attenuation = 2 dB
 - ii) Passband edge frequency = 200 rad/sec
 - iii) Minimum stopband attenuation = 20 dB
 - iv) Stopband edge frequency = 100 rad/sec. (10 Marks)
- b. Design a Cheebyshev analog lowpass filter that has – 3dB cutoff frequency of 100 rad/sec, and a stop band attenuation of 25 dB or greater for all radian frequency past 250 rad/sec. (10 Marks)
- 7 a. Explain why windows are necessary in FIR filter design. What are the different windows in practice? Explain the design procedure for the design of FIR filters using windows. (12 Marks)
- b. Design an FIR (low-pass) filter using rectangular window with passband gain of 0 dB, cut-off frequency of 200 Hz, sampling frequency of 1 KHz. Assume the length of the pulse response as 7. (08 Marks)
- 8 a. Distinguish between the analog and digital filters. (08 Marks)
- b. Explain the architecture of TMS 320 C 5X processor, with a neat diagram. (12 Marks)
